A Research on the Load Calculation Method in Designing the Traction Power Supply for Integrated Subway – MCR

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ABSTRACT
This paper presents a load calculation method in the design of a traction power supply for integrated subways. Integrated subways have a large carrying capacity and the ability to balance between meeting travel needs and satisfying conditions such as high quality service, cost optimization for railway infrastructure construction, and installation of traction power systems. In an integrated model, the calculation of the traction power supply design is much more complicated than in other stand-alone models. This paper presents the research results on the load calculation method of a traction power supply for the operation of the system. The results show the feasibility of the method when applied to an asynchronous loading system and met the standards of IEEE P1653.2, EN 50328, and IEC 60146-1 in the design of the power supply for permitted overloads according to class VI.

Keywords: urban rail transit; integrated urban railway; traction power supply; integrated subway

I. INTRODUCTION
A sustainable integrated urban transport system, with the large-scale interaction of various public transportation modes, attracts users with its friendliness, comfort, and time- and cost-saving in commuting and providing full "door-to-door" public transportation services. Urban rail is an indispensable part of a sustainable integrated urban transport system. However, different integrated solutions have been recommended depending on the type of transportation. A system with a large transport capacity integrating subway and suburban railway is needed to meet the large commuting needs connecting suburban areas and city centers. This system should operate with a very high transport capacity during peak hours, which is difficult to achieve separately for each type of transportation, and return to normal operating conditions during non-peak hours with low construction investment cost. The benefits of an integrated subway system are highlighted in [1-4]. To ensure that the system operates as flexibly, optimally, reliably, and energy-efficiently as desired, it needs to have a strong power supply system to meet the highest transport capacity during peak hours. However, most past studies focused on planning, forecasting, and addressing transport capacity, energy saving, and evaluating the benefits it brings to the comprehensive development of smart cities under the new context of integrated subways [5-10]. Therefore, this study focuses on calculating the design load for the power supply to enable the flexible operation of the system according to IEEE P1653.2, EN 50328, and IEC 60146-1 standards with an allowable overload of up to level VI. Matlab R2017b/Railway Systems software was used for computations and simulations.

II. INTEGRATED LOAD CALCULATION METHOD
A. Integrating Subway and Suburban Railway.
Integrated subway (ME) and suburban railway (CR) is a method of combining the transportation capacity of suburban railways by operating on subway travel corridors during peak hours (MCR). This method allows increased transport capacity and service frequency without the need to increase the number of trains operating on it. On the other hand, suburban trains operate like subway trains when running on the line. Figure 1 describes the integrated train running chart, in which A to E are the terminal stations of the subway line, B to E (or B to A but stops at any station) the terminal stations of the suburban railway, and B to A is the integrated peak-hour suburban railway station. Therefore, with this capability, passengers can travel continuously from the suburbs to the city center and stop at any station without having to change lines. At the same time, using suburban trains to meet the required number of trains during peak hours reduces the cost of purchasing train fleets. This is a typical example of integration: if the individual frequency for each type is 300s (a train appears at each station every 300s), then it will be 150s (a train appears at each station every 150s) when combined in an interleaved manner. If not integrated, relying on the combination of suburban trains stopping at all stations for the demand of subway transportation, the service frequency (headway) of the subway trains would need to be increased to
meet the demand, increasing the number of trains running on 
the section and the trains in reserve, which increases all related 
costs, such as purchasing trains, operation, maintenance, etc.

B. Load Calculation Method

There are many methods to calculate the design load for 
supplying electric traction power to subway or suburban 
railway systems [11-20]. However, these methods allow 
separate calculations for each system. For an integrated system, 
which is a combination of two systems with different capacities 
on the same power supply system, the difference is the train 
load, which is an important issue in load calculations. As the 
carrying capacities of subway and suburban railway systems 
are different, the train current used is also different. Correspondingly, the mechanical resistance \((R_m)\), the 
acceleration resistance \((R_a)\), acceleration, and operation speed 
are also different. The result is that the maximum instantaneous 
traction force for each train trip between two passenger stations 
is different. For a train to move, it needs to be provided with 

\[ \sum F_R = \sum p_{tr} s_{tr} \]

(1)

where \(p_{tr}\) is the train load that the power needs to supply in both directions can be calculated.

The integrated train running chart during peak hours is given by:

\[ M_x = n_x M_{d,x} + m_x M_{c,x} \]  
\[ M_{d,x} = \left( p_{d,x} f_{s,d,x} S_{d,x} + f_{s,d} \right) m_p + m_{d,x} \]  
\[ M_{c,x} = \left( p_{c,x} f_{s,c,x} S_{c,x} + f_{s,c} \right) m_p + m_{c,x} \]  

(3)  
(4)  
(5)

with criteria:

\[ \begin{align*}
4 < p_{d,x} &\leq 7, \, \text{p/m}^2 \\
4 < p_{c,x} &\leq 7, \, \text{p/m}^2 \\
1 < n_x &\leq 2, \, n_x \in \mathbb{Z}^+ \\
1 &\leq m_x, \, m_x \in \mathbb{Z}^+ \\
\end{align*} \]  

(6)

The weight of train \( y \) during peak hours is given by:

\[ M_y = n_y M_{d,y} + m_y M_{c,y} \]  
\[ M_{d,y} = \left( p_{d,y} f_{s,d,y} S_{d,y} + f_{s,d} \right) m_p + m_{d,y} \]  
\[ M_{c,y} = \left( p_{c,y} f_{s,c,y} S_{c,y} + f_{s,c} \right) m_p + m_{c,y} \]  

(7)  
(8)  
(9)

with criteria:

\[ \begin{align*}
4 < p_{d,y} &\leq 7, \, \text{p/m}^2 \\
4 < p_{c,y} &\leq 7, \, \text{p/m}^2 \\
1 < n_y &\leq 2, \, n_y \in \mathbb{Z}^+ \\
1 &\leq m_y, \, m_y \in \mathbb{Z}^+ \\
\end{align*} \]  

(10)

The components of train motion resistance within the 
power supply range of any traction substation \( i \) and along the \( j \)-th station route are:

\[ \sum F_R = \sum p_{tr} s_{tr} \]

(1)
Mechanical Resistance:
\[ R_{x,y} = A + Bv + Cv^2 \]  
(11)

Road curve [17]:
\[
\begin{align*}
R_{i,j} &= \frac{650}{r_{\text{SS}}}, r < 300 \\
R_{i,j} &= \frac{500}{r_{\text{SO}}}, r \geq 300
\end{align*}
\]  
(12)

Slope:
\[ R_{i,j} = \pm G/1000 \]  
(13)

Tunnel:
\[ R_{i,j} = \frac{f_{\text{a}}}{2} \]  
(14)

Acceleration drag:
\[ R_{x,y,i,j} = \frac{a_x}{g} \]  
(15)

The maximum resistance depends on the grade profile:
\[
\sum R_{i,j} = R_{i,j} + R_{i,j} + R_{i,j}
\]
\[ R_{\text{max},i,j} = \sum R_{i,j} < R_{i,j} + R_i \]  
(16)

The maximum instantaneous tractive force of trains x, y in each direction, within the supply range of a traction substation \( i \) and the route to the \( j \) station in the forward \( (h) \) and the backward directions \( (k) \) is:
\[
F_{i,j,-hx,ky,hy,ky} = M (R_{ax} + R_{rx} + \sum R_{ax,ax-ky})
\]  
(17)

\[
\sum R_{ax,ax-ky} = R_{ax,ax} + R_{ax,ax} + \sum R_{ax,ax-ky}
\]  
(18)

\[
F_{i,j,-hx,ky,ky,ky} = M (R_{ax} + R_{rx} + \sum R_{ax,ax-ky})
\]  
(19)

\[
\sum R_{ax,ax-ky} = R_{ax,ax} + R_{ax,ax} + \sum R_{ax,ax-ky}
\]  
(20)

\[
F_{i,j,-hx,ky,ky,hy} = M (R_{ax} + R_{rx} + \sum R_{ax,ax-ky})
\]  
(21)

\[
\sum R_{ax,ax-ky} = R_{ax,ax} + R_{ax,ax} + \sum R_{ax,ax-ky}
\]  
(22)

\[
F_{i,j,-hy,ky,ky,ky} = M (R_{ax} + R_{rx} + \sum R_{ax,ax-ky})
\]  
(23)

\[
\sum R_{ax,ax-ky} = R_{ax,ax} + R_{ax,ax} + \sum R_{ax,ax-ky}
\]  
(24)

Assuming that the integrated system operates with an equal service frequency for both \( x \) and \( y \) train lines on the route, the total maximum instantaneous traction force is determined based on the maximum instantaneous traction force in the power supply segment of an electric traction station in both directions, as follows:
\[
\sum_{i=1}^{j} F_{i,j, (na)\max} = 2 \cdot \sum_{i=1}^{j} p_{i,j} P_{i,\max} \cdot F_{i,j, (kx,hy,ky)\max}
\]  
(25)

In (24), it depends on the maximum allowable force \( c_{l,\max} \) of the transmission line:
\[
\left\{ \begin{array}{l}
\sum p_{i,j} P_{i,\max} = \frac{60}{c_{l,\max}} \cdot \frac{D_{\text{TPS}i}}{\text{s}_{\text{ce}}} \\\n1.5 \leq c_{l,\max} < c_{l,\text{MFE}} \cdot c_{l,\max} \leq \frac{c_{l,\max}}{c_{l,\max}}
\end{array} \right.
\]  
(26)

If there is a power outage at any substation disrupting the power supply, then:
\[
\sum_{i=1}^{j} F_{i,j, (er)\max} = 2 \cdot \sum_{i=1}^{j} p_{i,j} P_{i,\max} \cdot F_{i,j, (kx,hy,ky)\max}
\]  
(27)

where:
\[
\left\{ \begin{array}{l}
\sum p_{i,j} P_{i,\max} = \frac{60}{c_{l,\max}} \cdot \frac{D_{\text{TPS}i}}{\text{s}_{\text{ce}}} \\\n1.5 \leq c_{l,\max} < c_{l,\text{MFE}} \cdot c_{l,\max} \leq \frac{c_{l,\max}}{c_{l,\max}}
\end{array} \right.
\]  
(28)

Based on the force-velocity curve, the instantaneous maximum power requirement is calculated as a function of the force-velocity relationship. The power under normal operating conditions (na) and during an error (er) is:
\[
P_{i,j, (na)\max} = \sum_{i=1}^{j} p_{i,j} P_{i,\max} \cdot \frac{\text{s}_{\text{ce}}}{3.6 \cdot m_{\text{t,max}} \cdot m_{\text{r,max}}}
\]  
(29)

\[
P_{i,j, (er)\max} = \sum_{i=1}^{j} p_{i,j} P_{i,\max} \cdot \frac{\text{s}_{\text{ce}}}{3.6 \cdot m_{\text{t,max}} \cdot m_{\text{r,max}}}
\]  
(30)

with mechanical \( (m_{\text{t}}) \) and motor efficiency \( (m_{\text{r}}) \) conditions:
\[
\begin{align*}
\eta_{\text{m.t,min}} &< \eta_{\text{m,t}} \leq \eta_{\text{m,t,max}} \\
\eta_{\text{m.r,min}} &< \eta_{\text{m,r}} \leq \eta_{\text{m,r,max}} \\
v_{\text{ce}} &< v \leq v_{\text{peak}}
\end{align*}
\]  
(31)

The auxiliary consumption power used for purposes other than pulling force on each train type is calculated as follows:
\[
P_{i,x,y,\max} = \sum_{i=1}^{j} p_{i,x,y} P_{i,\max} \cdot \left( \eta_{i,x,y} P_{i,x,y} + m_{\text{t},\max} P_{i,\text{c},\max} \right)
\]  
(32)

\[
P_{i,x,y,\max} = \sum_{i=1}^{j} p_{i,x,y} P_{i,\max} \cdot \left( \eta_{i,x,y} P_{i,x,y} + m_{\text{t},\max} P_{i,\text{c},\max} \right)
\]  
(33)

The maximum power consumption under normal operating conditions and when an error occurred at station \( i \) are calculated as:
\[
P_{i,j, (na)\max} = P_{i,j, (na)\max} + P_{i,j, (er)\max}
\]  
(34)

\[
P_{i,j, (er)\max} = P_{i,j, (er)\max} + P_{i,j, (er)\max}
\]  
(35)

Equations (36) and (37) give the maximum power consumption required to be supplied if there is regenerative braking (energy returned during braking) under normal operating conditions and when an error occurs. The percentage of the energy recovered \( (\eta_{\text{re}}) \) depends on the frequency of service and the voltage of the traction system:
\[
P_{i,j, (re)\max} = P_{i,j, (na)\max} + P_{i,j, (er)\max}
\]  
(36)

\[
P_{i,j, (re)\max} = P_{i,j, (na)\max} + P_{i,j, (er)\max}
\]  
(37)

With the condition based on the type of service:
\[
\begin{align*}
\eta_{i,\text{re,na, min}} &< \eta_{i,\text{re,na, max}} \\
\eta_{i,\text{re, er, min}} &< \eta_{i,\text{re, er, max}}
\end{align*}
\]  
(38)

The power selection for the traction substation is:
\[
P_{i,j, (na)\max} = P_{i,j, (na)\max}
\]  
(39)

\[
P_{i,j, (er)\max} = P_{i,j, (er)\max}
\]  
(40)

The power of the traction substation selected according to (35) and (36) must comply with the IEEE P1635.2, EN 50328, and the IEC 60146-1 standards.
III. SYSTEM DESIGN

A. Load Parameters

TABLE I. THE PROFILE OF THE ROUTE FROM TRACTION SUBSTATION NO. 3 TO NO. 4 ALONG THE LINE

<table>
<thead>
<tr>
<th>Km</th>
<th>TPSi</th>
<th>Stf</th>
<th>G_{w.e}</th>
<th>C</th>
<th>Rt</th>
</tr>
</thead>
<tbody>
<tr>
<td>10.0</td>
<td>SP</td>
<td>11</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11.00</td>
<td></td>
<td>12</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11.50</td>
<td>+35</td>
<td>650</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>12.00</td>
<td></td>
<td>13</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>12.40</td>
<td>3</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>13.70</td>
<td></td>
<td>+5</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14.00</td>
<td>SP</td>
<td>15</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15.40</td>
<td>16</td>
<td>-5</td>
<td>17.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15.80</td>
<td></td>
<td>-20</td>
<td>17.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>16.00</td>
<td>4</td>
<td></td>
<td>17.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>16.40</td>
<td>17</td>
<td></td>
<td>17.14</td>
<td></td>
<td></td>
</tr>
<tr>
<td>17.40</td>
<td>18</td>
<td></td>
<td>17.14</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

TABLE II. LOAD PARAMETERS

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Units</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>C_{p,t}</td>
<td>[p/h/d]</td>
<td>45,000</td>
</tr>
<tr>
<td>C_{S,t}</td>
<td>[p/h/d]</td>
<td>54,000</td>
</tr>
<tr>
<td>m_{n,x}</td>
<td>[m^3/s^2]</td>
<td>0.9/1.0</td>
</tr>
<tr>
<td>m_{n,y}</td>
<td>[m^3/s^2]</td>
<td>0.85/1.0</td>
</tr>
<tr>
<td>R_{x,R}</td>
<td>[kg/ton]</td>
<td></td>
</tr>
</tbody>
</table>

B. Load Calculation Process

The flowchart of the load calculation process is shown in Figure 3.

IV. RESULT AND DISCUSSION

A. Results of Load Calculations

The train parameters that have the carrying capacity to meet the demand of the line described in Table III are selected. The trains have the maximum passenger capacity including fixed seats and standing passengers of 7p/m^2 in both stages. In stage 1, the demand for transportation is 45,000p/h/d and the supply capacity is 45,774p/h/d with a headway of 3p/t/d. In stage 2, the demand for transportation is 54,000p/h/d and the supply capacity is 54,929p/h/d with a headway of 2.5p/t/d. To meet the different demands in each stage in this design, the system only changes the service frequency (the time interval between train services) without changing the structure or carrying capacity. Therefore, with the maximum carrying capacity according to the stages, the subway train x weighs 224.97 tons and the suburban train y weighs 211.68 tons.

B. Calculation Results of Traction Force

Consider a section of the line between two traction substations with a complex railway track from station ST11 to ST18, as shown in Table I. Under normal operation, TPS3 supplies power from station ST11 to ST14, while TPS4 supplies power from station ST15 to ST18. Assuming that TPS4 experiences a disruption in its power supply, TPS3 will have to provide power to its section and a portion of the adjacent station, from station ST11 to ST16. The following scenarios may occur:

In case 1, the traction force and train speed curves vary depending on whether the train is moving in the direction of the power supply or the opposite one. In normal operation, when both TPS3 and TPS4 are supplying power to the trains, the maximum required traction force is reached when the trains...
accelerate in both the forward and backward directions at the stations. The maximum required traction force for the outer suburban train $F_{y,na,max}$ is 205.69kN, and for the metro train $F_{x,na,max}$ is 233.46kN. In the event of a TPS4 power outage, TPS3 is required to supply power to the trains along its section as well as a part of the adjacent substation from ST11 to ST16. The maximum required traction force for the suburban train $F_{y,er,max}$ is 216.07kN, and for the metro train $F_{x,er,max}$ is 244.5kN. Overall, in case 1, the curves of traction force and train speed are relatively similar for both the outer suburban and metro trains. The maximum required traction force increases slightly in the event of a TPS4 power outage, but the difference is not significant. The train speed also changes slightly within the power supply range of a traction substation, but this change is not enough to impact the train operation.

In case 2, both TPS3 and TPS4 supply power to trains operating on the interacting section. The required traction force distribution in the described section is shown in Figure 5. Under normal operating conditions, TPS3 supplies power only to the traction force required when the train accelerates at the departure and arrival stations of the suburban train. The maximum required traction force for the suburban train $F_{y,na,max}$ is 205.69kN. In the event of a TPS3 malfunction, it must supply power to the required traction force for the train acceleration at the departure and arrival stations in the tunnel. The maximum required traction force for the suburban train $F_{y,er,max}$ is 216.07kN and for the subway train $F_{x,er,max}$ is 244.5kN. In terms of speed, when TPS4 is in normal operation, it supplies power to the trains in the described section. Therefore, the speed curve is smooth and not affected by the power supply. However, in the event of a TPS4 malfunction, the power supply to the trains in this section will be affected, which may result in a decrease in their speed.

V. CONCLUSION

This paper presented the results of a study on a method for calculating the maximum instantaneous pulling force to predict the instantaneous power consumption of loads for the design of power stations in integrated subway train models - MCR. The method was designed and simulated using Matlab R2017b/Railway Systems software, with a variety of load cases for maximum power consumption during peak hours in different stages and different situations to demonstrate its reliability. In addition, the method also demonstrates transparency and logic in calculating data according to a sequence with filtering and comparison for contingency situations to avoid power wastage. The calculated power compared to the minimum and maximum load requirements was 14.67% and 21.81%, which is suitable for station power that meets the standards of IEEE P1653.2, EN 50328, and IEC 60146-1 for redundancy coefficients. Finally, the proposed method of calculation is a reliable and cost-effective scientific approach in the study of designing the power supply for subway trains.

REFERENCES


