A Distributed Control Approach for Demand Response in Smart Grids

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Abstract—The smart grid is a new concept that has been developed during recent years to improve the intelligence and efficiency of electric power system management. Traditional electricity systems are combined and integrated with information technology, communication technology, and intelligent control technology in the smart grid. Demand Response (DR) refers to the changes in consumers' electricity consumption behavior in response to dynamic pricing or financial incentives. Based on the control manner, DR methods are classified as centralized or distributed. In distributed techniques, customers communicate with the other consumers and provide data to the power utility about the overall use. In this paper, we focus on the distributed approach of DR using the shifting method for a short-term horizon. To be more specific, three well-known solutions were studied: the Resource Allocation with Legitimate Claims, the Constrained Fair-Splitting Dispatch, and Real-Time Pricing. Finally, we compare the different techniques of DR distributed approaches based on the control mechanism.

Keywords—demand response; distributed approach; resource allocation with legitimate claims; constrained fair-splitting dispatch problem; real-time pricing

I. INTRODUCTION

Demand Response (DR) is a technique describing the way the demand side responds to the supply-side price techniques or incentive measures [1-3]. DR leads to modifications in end-use customer consumption patterns as a result of the changes in electricity pricing over time or incentive payments designed at encouraging lesser energy use during periods when the market prices are higher or when system reliability is affected. DR is a cost-effective way to minimize power usage, and the cost of putting it in place is less than the cost of adding more generation capacity to get the same result [4]. The fundamental advantage of DR is that it improves power system use by establishing a closer relation between customers' consumption and the electricity price [5]. DR is becoming increasingly crucial in the interaction between supply and demand, which is the most critical aspect of the smart grid compared to traditional power systems. When consumers participate in DR programs, they are more likely to decrease their electricity use during critical peak periods or shift some peak demand to off-peak periods [6]. As a result, the economy and security of the electricity systems are improved. Customers can react to high prices in one of the following methods [7]:

• Foregoing is a method for limiting electricity consumption during times of high prices, but not consuming it thereafter.
• Shifting is a technique to reschedule power usage from high-priced periods to other times.
• Onsite generation is a method where some users have backup emergency generators that can be used to respond partially or totally to their use demands.

In this paper, we are interested in the shifting method as it is the most used in DR.

DR methods are classified as centralized and distributed, based on their control mechanism. In the centralized approach, customers interact directly with the power utility, without communicating with each other. In the distributed approach, consumers communicate with the others and inform the power utility about its use [8]. The main contributions of this paper are: (1) the introduction and exhibitions of results of the most famous distributed solutions for DR using the short-term horizon shifting method, (2) addressing a comparison between the distributed solutions.

II. BACKGROUND

DR methods are classified as centralized or distributed, based on the control mechanism. In centralized DR, the response decisions for energy assignment or load scheduling are solely handled by the power utility, based on groups formed by sets of customers. In this method, each consumer participates without having to be aware of the other customers in the group's involvement [9]. Furthermore, fixing the problems centrally necessitates transferring all the consumers' personal data to the aggregator, resulting in significant communication overhead and privacy problems. This central strategy, on the other hand, always entails a large computational load along with the privacy issue. In the
distributed approach, the power utility’s key role is the delivery of pricing information, depended on the total system consumption. Customers can manage directly with one another to accomplish aggregated load reduction. Unlike a central authority which collects data to make decisions, the decentralized control ensures scalability and protection of consumer privacy [10]. In the literature review, there were found two primary families on distributed DR approaches. The first group includes techniques that treat energy uses as continuous [11] which makes the underlying DR issue convex and hence computationally feasible. The second group includes techniques representing energy uses as a combination of discrete and continuous uses [12].

The interaction between consumers and providers can be divided into 3 approaches based on the time scale: long-term horizon, medium-term horizon, and short-term horizon. Price-based demand response is concerning customers’ energy consumption changes in reaction to changes in their purchase prices [13]. This category includes Real-Time Pricing (RTP), Time-Of-Use (TOU), and Critical-Peak Pricing (CPP). For RTP, electricity prices are set for a short-term horizon of time, usually one hour [14], to match fluctuations in wholesale electricity prices. Customers are frequently given price information a day or hour ahead of time. TOU defines different electricity prices. Customers are given the option to manage their consumption without using power costs. Instead, customers agree to reduce their load during crucial circumstances and to request power required, \( \pi_{i,t} \) in accordance to the system’s state, if it is critical. In this section, we present the most important techniques related to DR of smart grid as distributed approach.

A. Resource Allocation with Legitimate Claims (RALC)
In RALC, the provider agent must determine how much energy \( \pi_{i,t}^{\text{in}} \) each customer agent should be assigned, taking into account certain limits. As a result, the energy demand allocation problem is to consider how much energy should be allocated to each customer agent \( \pi_{i,t}^{\text{min}}, \pi_{i,t}^{\text{max}} \). The proposed allocation method is based on distributive fairness and is self-organized [21]. Customer agents agree on the criteria for conducting the allocation. Any of the provider agents then computes this allocation. The allocation is done pursuant to a set of canons in distributive justice. To this purpose, we propose the following mechanism for agreeing on load allocation at a certain time \( t \) (hour):

1. Information about the load \( L(t) \) is available at the provider agent (\( t \)).
2. Every customer agent \( i \) sends a request to the provider agent asking the desired power \( \pi_{i,t}^{\text{req}} \) as well as the constraints \( \pi_{i,t}^{\text{min}}, \pi_{i,t}^{\text{max}} \).
3. The provider agent calculates the total amount of power requested \( \pi_{i,t} \), \( \pi_{i,t}^{\text{min}}, \pi_{i,t}^{\text{max}} \). There could be a variety of scenarios:
   - \( L_i = \pi_{i,t}^{\text{min}} \): If the equality holds, all customer agents are given the smallest amount of authority, \( \pi_{i,t}^{\text{in}} = \pi_{i,t}^{\text{min}} \).
   - \( \pi_{i,t}^{\text{min}} \leq L_i \leq \pi_{i,t}^{\text{max}} \): Customer agents are assigned power within their needed range. Each customer agent’s power is assigned by the provider agent based on a rank attributed according to a set of weights. Weights are assigned to all customer agents after they reached an agreement a set of canons. In this case, every customer receives power \( \pi_{i,t}^{\text{in}} \) such that:
     \[
     \pi_{i,t}^{\text{in}} \leftarrow \pi_{i,t}^{\text{min}} + \min(L_i - \pi_{i,t}^{\text{min}}, \pi_{i,t}^{\text{max}} - \pi_{i,t}^{\text{min}})
     \]
   - \( L_i \geq \pi_{i,t}^{\text{max}} \) The customer agent obtains the exact amount of power required, \( \pi_{i,t}^{\text{in}} = \pi_{i,t}^{\text{in}} \).
4. The provider agent provides each customer agent with the computed allocation \( \pi_{i,t}^{\text{in}} \).
5. Each customer agent must pay \( \lambda \times \pi_{i,t}^{\text{in}} \) in accordance to the provided energy \( \pi_{i,t}^{\text{in}} \).

The second protocol in step 3 is crucial, as it requires the customer agents to agree on the way the load will be divided. To do so, the Rescher’s canons are used as voting functions \( f \) for the allocation, and the relevance of each function is decided by its associated weight \( w \). The process of determining the way the load is divided is essentially an allocation procedure that is frequently applied. The weights’ initial value is set at \( w_i = \frac{1}{m} \) (where \( m \) represents the functions number), and the procedure proceeds as follows:

A consensus on a particular ranked list of customer agents should be reached in order to proceed with the allocation. The
Borda count protocol is used as a consensus-based voting approach. In the Borda count process, each function \( f^* \) is considered as a voter. Each vote in Borda count voting sorts the candidates based on a specific criterion. Each candidate in the list is given Borda points: for example, if we have \( n \) customer agents, then the rank \( k \) receives \( n - k + 1 \) Borda points. The Borda points obtained from each vote are added together to give a total Borda score for every agent. The candidate having the highest Borda score gains the Borda count procedure, however it is possible to find several “winners,” therefore we construct a Borda point queue in decreasing order and assign electricity to the head of the queue until there are no more to allocate. Under a set of functions \( F \), the Borda score \( B \) of candidate \( i \) is calculated by:

\[
B(i, F) = \sum_{i=1}^{f} w_i \times bpts(f, (i))
\]  

where \( f(i) \) determines each \( f^*_i \)'s rank order for candidate \( i \), \( bpts() \) computes the Borda points for that rank, and \( w_i \) is the weight associated with the function \( f_i \).

The Borda count function returns the Borda ptq list after computing the Borda score \( B \) for each agent. Algorithm 1 presents the main idea explained above, where \( A \) is a set of \( N \) Consumer agents, and \( F \) is a set of \( m \) voting functions \( f^*_i \) each with its own weight \( w^*_i \).

**Algorithm 1. Resource Allocation with Legitimate Claims.**

1: For each time slot \( t \in T \) do
2: \( \pi_i \leftarrow 0 \), \( \pi^\text{min}_i \leftarrow 0 \)
3: for each customer agent \( i \in N \) do
4: \( \pi_i \leftarrow \pi_i + \pi^\text{max}_{ij} \)
5: \( \pi^\text{min}_i \leftarrow \pi^\text{min}_i + \pi^\text{min}_{ij} \)
6: end for
7: \( L_t \leftarrow \text{update}(L_t) \)
8: if \( L_t > \pi^\text{min}_i \) then
9: for each customer agent \( i \in N \) do
10: \( \pi^\text{ret}_i \leftarrow \pi^\text{ret}_i \)
11: end for
12: Else if \( L_t > \pi^\text{max}_i \) then
13: rank orders \( \leftarrow \text{[/]} \)
14: for every voting function \( f^*_i \in F \) do
15: rank orders \( \leftarrow \text{rank orders \cup f(A)} \)
16: end for
17: Borda ptq \( \leftarrow \text{Borda count(rank orders, F)} \)
18: repeat
19: \( i \leftarrow \text{head(Borda ptq) \// customer i} \)
20: Borda ptq \( \leftarrow \text{tail(Borda ptq)} \)
21: \( \pi^\text{ret}_i \leftarrow \pi^\text{ret}_i + \min(L_t - \pi^\text{max}_{ij}, \pi^\text{min}_{ij} - \pi^\text{min}_{ij}) \)
22: \( L_t \leftarrow L_t - \pi^\text{ret}_i \)
23: until \( \text{Borda ptq = Null} \)
24: else \( \text{L_t = \pi^\text{min}_i} \) then
25: for each customer agent \( i \in N \) do
26: \( \pi^\text{ret}_i \leftarrow \pi^\text{ret}_i \)
27: End for
28: End if
29: End for
30: End

As a running example, Figure 1 depicts the agents ranked by a group of voters, each of whom creates its own rank list. Borda points are assigned to each rank in a list and then are combined together in a weighted sum to produce a single final rank list and final Borda score for each agent.

**B. Constrained Fair-Splitting Dispatch (CFSD)**

 SFSD is the most famous DR method. At first, we consider a direct graph \( G = \{V, E\} \) where each customer \( i \) can possibly transmit information to other customers called neighbors \( N_i \). The customers sending data (respectively receiving data) to the customer \( i \) are called the in-neighbors (respectively out-neighbors) of \( i \) and are represented by the set \( N^+_i \) (respectively \( N^-_i \) ) \( \{j \in V: (i, j) \in E\} \). The number of in-neighbors (respectively out-neighbors) of agent \( i \) is called the in-degree (respectively out-degree) and is denoted by \( D^+_i \) (respectively \( D^-_i \)). \( D^i \) denotes the total amount of power that the system should collectively deliver, i.e.: \( D^i = \sum_{i=1}^{N} \pi_i \). The ratio consensus technique is explained below. Consider the exchange of data between customers in a direct graph where each customer \( i \) in the graph keeps two values, \( y_i \) and \( z_i \), called internal states, which are independent and updated as a linear combination of customer \( i \)'s prior internal states and the past internal states of its in-neighbors respectively. For each \( k \geq 0 \), each customer \( i \) updates \( y_i \) and \( z_i \) in the following way [22]:

\[
y_i(k+1) =\sum_{j \in N^+_{i}} \frac{1}{D_j} y_j(k) \quad (2)
\]

\[
z_i(k+1) =\sum_{j \in N^-_{i}} \frac{1}{D_j} z_j(k) \quad (3)
\]

\[\forall k, \text{customer } i \text{ computes:} \]

\[
y_i(k) = \frac{y_i(k)}{z_i(k)} \quad (4)
\]
Lemma 1: For every customer $i$, it is demonstrated in [22] the convergence of $\gamma_i(k)$ to some constant $\gamma$.

Then, each customer $i$ asymptotically obtains:

$$\gamma = \lim_{k \to \infty} \gamma_i(k) = \lim_{k \to \infty} \frac{\sum_{j=1}^{n} y_{j}(0)}{\sum_{j=1}^{n} z_{j}(0)}$$ (5)

Without loss of generality, we assume that the total resource amount $\Pi$ is known to a power entity $V$, who is able to exchange data with specific customers $V$ (having a number $m$). Besides, the initial conditions in (2) are set to $y_i(0) = \Pi/m - \pi_{i}^{\text{min}}$ if $i \in V^c$, and $y_i(0) = -\pi_{i}^{\text{min}}$ otherwise. Moreover, the initial conditions in (3) are set to $z_i(0) = \pi_{i}^{\text{max}} - \pi_{i}^{\text{min}} \cdot \forall i$. Then, as long as $\sum_{i=1}^{n} \pi_{i}^{\text{max}} \leq \Pi \leq \sum_{i=1}^{n} \pi_{i}^{\text{max}}$, we conclude from Lemma 1 that the $i$-th node can asymptotically determine its contribution $\pi_{i}^{\text{opt}}$ as:

$$\pi_{i}^{\text{opt}} = \pi_{i}^{\text{min}} + \gamma (\pi_{i}^{\text{max}} - \pi_{i}^{\text{min}})$$ (6)

where:

$$\gamma = \lim_{k \to \infty} \gamma_i(k) = \lim_{k \to \infty} \frac{\sum_{j=1}^{n} y_{j}(0)}{z_{j}(0)} = \frac{\Pi - \sum_{j=1}^{n} \pi_{j}^{\text{min}}}{\sum_{j=1}^{n} (\pi_{j}^{\text{max}} - \pi_{j}^{\text{min}})}$$ (7)

Note that (6) satisfies $\pi_{i}^{\text{opt}} < \pi_{i}^{\text{opt}} < \pi_{i}^{\text{max}}$, $\forall i$, and also $\sum_{i=1}^{n} \pi_{i}^{\text{opt}} = \Pi$. Additionally, every customer $i$ can independently declare infeasibility if $\gamma > 1$ or $\gamma < 0$. The solution in (6) is not considered as the optimal solution, but it ensures a "fair" splitting of the total amount of resource $\Pi$ proportional to the "excess" capacity of each node.

As a running example, Figure 2 depicts the convergence of $\gamma_i(k)$ for $j = 1, ..., 4$ over 30 iterations. We can conclude from the graph that after about 13 iterations, all customers obtain a common value $\gamma = 0.9$. As a result, the customers decide the solution is possible and update their output in accordance with (6), obtaining $x = [0.279, 0.129, 0.364, 0.228]^T$.

C. Real-Time Pricing (RTP) Algorithm

The provider agent modifies its energy supply tactics in every iteration, based on the consumer agents' energy consumption strategies, whereas the consumer agent $i$ adjusts its energy consumption based on real-time costs (see Figure 3). We present here the Optimal RTP algorithm based on the utility maximization for smart grid [23] in which:

$$\pi_{i,j}^{\text{opt}}$$ is the optimal requested power by the consumer agent $i$ to the provider agent $j$, $\lambda_{j}^{*}$ is the updated price by the provider agent $j$, $L_{j}(\lambda_{j})$ is the capacity update, and $\mu_{j}$ the coordination parameter. The requested power is:

$$\pi_{i,j}^{\text{opt}}(\lambda_{j}^{*}) = \arg \max_{\pi_{i,j}^{\text{opt}}} U(\pi_{i,j}^{\text{opt}}, \omega_{j}) - \lambda_{j}^{*} \pi_{i,j}^{\text{opt}}$$ (8)

and the price update is provided by:

$$\lambda_{j}^{*} = \left[ \lambda_{j}^{*} + \gamma \left( \sum_{i=1}^{n} \pi_{i,j}^{\text{opt}}(\lambda_{j}) - L_{j}(\lambda_{j}) \right) \right]^{-1}$$ (9)

where $[x]^+$ is the maximum of $\{x; 0\}$.

The capacity update is given by:

$$L_{j}(\lambda_{j}) = \arg \max_{\lambda_{j}} \lambda_{j}^{*} L_{j} - C_{j}(L_{j})$$ (10)

and the coordination parameter by:

$$\mu_{j} = \left[ \mu_{j}^{*} - \gamma \left( \sum_{i=1}^{n} \pi_{i,j}^{\text{opt}}(\lambda_{j}) - b_{j} \right) \right]^{-1}$$ (11)

1) Real-Time Pricing Formulation

Algorithm 2: Executed at consumer agent $i$.

1: for $t \in T$
2:   Receive the new price $\lambda_{j}^{*}$ from the provider agent $j$.
3:   Compute the consumption value $\pi_{i,j}^{\text{opt}}$ using (8).
4:   Send the updated $\pi_{i,j}^{\text{opt}}$ to the provider agent $j$.
5:   Calculate the coordination parameter $\mu_{j}^{*}$ by (11).
6: end for

Algorithm 3: Performed by the provider agent $j$.

1: repeat
2:   if time $t \in T$
3:      Calculate the new electricity price $\lambda_{j}^{*}$ by solving (9).
4:      Send the new price $\lambda_{j}^{*}$ to each consumer $i$.
5:   else
6:      Update the capacity value $L_{j}(\lambda_{j})$ using (10).
7:      Receive $\pi_{i,j}^{\text{opt}}$ from all the consumer agents $i \in N$.
8:      Update the total load $\sum_{i=1}^{n} \pi_{i,j}^{\text{opt}}$ accordingly.
9: end if
10: until the end of planned period.

The pricing mechanism proposed in this study aims to align social benefit with individual welfare, i.e. to find a suitable pricing so that the locally optimal solution is the same as the
globally optimal solution. From the Algorithm 2, the consumer agents are regarded independent agents who are responsible for their own well-being. To improve their benefits and contentment, each consumer agent requires a specific quantity of power. The mission of a smart grid is to manage the coordination of the customer agents to cover the requested power, so that there is a balance between energy production and consumption. Form the Algorithm 3, it is clear that the provider agent is trying to fulfill the consumer agents' requests or facilitate the coordination between customer agents so that they can guarantee the total requested power and maintain a balance between energy production and consumption (in accordance with the consumer agents' needs and constraints). The following characteristics are included in the proposed algorithms.

- Algorithms 2 and 3 are considered distributed algorithms in which each utility company and user solves the subproblems locally to allocate energy. There is no requirement for a central controller or a third party.
- Each user helps energy allocation by coordinating the demand from several power entities to satisfy his need.
- The distributed Algorithms 2 and 3 protect power entities' and customers' privacy. However, this leads to a more complicated solution.

Figure 3 depicts the communication between the utility company and the user in a multiseller–multibuyer system. The electricity pricing and energy demand are the two pieces of information that must be exchanged between the utility provider and the customer. Algorithms 2 and 3 summarize the distributed algorithms at each utility business and each user respectively. Each utility business adjusts its supply in response to the electricity price. Each utility company determines the price of power depending on its supply and demand from all customers. The price is then made public to all users. The electricity price and the user's coordination parameter are used to update each user's demand.

2) Running Example

Figure 4 depicts the relationship between the provider's hourly fee and the consumed electricity. Customers actually lower their use during peak hours (as shown in the Figure at hours 18 and 19) because the price is doubled. Furthermore, clients determine the optimal consumption at the lowest price (in the Figure at hours 11 and 12): this is illustrating the most significant benefit of the RTP algorithm.

IV. NUMERICAL RESULTS

Through this section, we study the features of each technique: DR with RALC, CFSD, and the RTP algorithm. Some numerical results illustrating the results of each are provided and compared. For the purposes of simulation throughout our research, we will use a network with $C = 7$ companies and $U = 150$ clients.

Figures 5 and 6 show the customers' average utility and energy usage as functions of the timeslots required for all comparative frameworks to converge to the steady customers' association with power companies. The results show that the RTP algorithm produces the highest consumer utility (Figure 5) and the lowest customer electricity consumption (Figure 6). This trend is the result of the use of (8)-(10), including both monetary and electricity-related aspects, as described above. Furthermore, the RALC, which is self-organized and based on distributive fairness, delivers acceptable outcomes in terms of consumers' utility and electricity consumptions. CFSD, on the other hand, does not optimize the electricity consumption and achieves the lowest customers' utility and high electricity consumption. When compared to the other two algorithms, the RTP algorithm outperforms both, demonstrating the huge benefit of using optimization in the overall process. The results reveal that: (a) The CFSD applies no optimization. Users choose time periods at random to place their schedulable loads. (b) The RALC is a greedy algorithm, in which everyone strives to reduce its total electricity cost by lowering the base price. This one simulates a scenario in which there is no cost fluctuation fee and users do not collaborate while making judgments. (c) The RTP algorithm provides optimal results.
future work, it is possible to extend the distributed algorithms as well as the lowest customer electricity consumption. The results show that the RTP technique is the best as it ensures the highest consumer utility and energy usage. The results show that the RTP compared these techniques based on two criteria: customers’ reaction time. In this paper, we studied the most widely known services like frequency regulation, which has a faster scale response to peak power constraints as well as for auxiliary market efficiency. It can be used to lower the overall load in allowing better system operation and extension, and increased market efficiency. It can be used to lower the overall load in response to peak power constraints as well as for auxiliary services like frequency regulation, which has a faster scale reaction time. In this paper, we studied the most widely known techniques in distributed DR, namely RALC, CFSD, RTP. We compared these techniques based on two criteria: customers’ average utility and energy usage. The results show that the RTP technique is the best as it ensures the highest consumer utility as well as the lowest customer electricity consumption. For future work, it is possible to extend the distributed algorithms to make them robust to faulty consumers.

V. CONCLUSION

DR is an important subject in smart grid implementations, allowing better system operation and extension, and increased market efficiency. It can be used to lower the overall load in response to peak power constraints as well as for auxiliary services like frequency regulation, which has a faster scale reaction time. In this paper, we studied the most widely known techniques in distributed DR, namely RALC, CFSD, RTP. We compared these techniques based on two criteria: customers’ average utility and energy usage. The results show that the RTP technique is the best as it ensures the highest consumer utility as well as the lowest customer electricity consumption. For future work, it is possible to extend the distributed algorithms to make them robust to faulty consumers.

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