Numerical Investigation of the Physical Properties Effect on the Thermal Performance of a Vertical Geothermal Heat Exchanger

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Abstract—Low-temperature geothermal energy is a promising technique for heating and cooling residential and commercial premises, especially since it is one of the green energy solutions that respect the environment. The principle of this technique is based on thermal exchange between the heat pump and the basement using a vertically buried heat exchanger. This is usually made of a U-shaped tube inserted vertically in a borehole made in the ground and filled with a filler material. The purpose of the present study is to vary the different construction materials of the U-tube, the filling material and the soil, in order to obtain the most energy-efficient parameters. The evolution of temperature and heat flux as a function of time has been highlighted for different combinations. Knowing that an experimental study requires a considerable monetary fund, the present model has been validated using previously literature results. Recommendations on the choice of different materials of the geothermal heat exchanger are proclaimed at the end of this work.

Keywords—geothermal energy; heat exchanger; finite volumes; temperature; heat flux

I. INTRODUCTION

Seasonal storage systems of solar energy by geothermal well (SSGW) that use the ground as a heat source is a promising and highly efficient renewable energy technology to provide heating and cooling of residential and commercial buildings and sanitary hot water [1, 2]. This system is generally composed of a heat pump, a solar thermal panel, a geothermal heat exchanger and a system for heat distribution in the building (radiators or heating floor), see Figure 1. These systems offer better levels of comfort, reasonable environmental safety, reduced greenhouse gas emissions and reduced noise levels [3]. In an area between 5 and 45 meters deep, the soil is at a constant temperature throughout the year: warmer than the ambient temperature in winter and cooler in summer [4]. The geothermal heat pump allows to collect heat from the building and to inject it into the ground during the summer and to transfer the heat stored in the ground to the building during the winter [5]. The system uses the ground as a heat source when operating in heating mode while in cooling mode, it uses the soil as a heat sink [1]. Currently, the SSGW is a high-performance and economical technology for heating and cooling buildings. Most geothermal heat pumps use vertical buried heat exchangers. They offer better energy performance compared to horizontal heat exchangers because of the small temperature fluctuations generated in the ground.

All geothermal heat exchangers (GHEs) generally consist of a U-tube pipe disposed in a known deep borehole. The boreholes have typical diameters ranged from 76mm to 127mm filled with a high thermal conductivity bentonite grout in order to ensure a good heat transfer between the fluid and the stock. The fluid enters the probe at a known temperature, the pipe diameter is in the range of 19mm to 38mm. The upper surface of the geothermal heat exchanger is free and in constant contact with the atmosphere [6]. Several works have been conducted to deal with the problem of heat transfer in the soil. Analytical models are typically based on the theory of the source line [7] or the cylindrical source [8]. These two models assume a source of infinite length in an isotropic medium, and they do not take into account the variation of the temperature at depth and the surface effects such as radiation and convection. On the other hand, several numerical and experimental studies have treated the vertical geothermal heat exchangers. Author in [9] has studied the problem of the thermal response of a multiple geothermal probes heat exchanger subjected to various conditions. Authors in [10] developed a numerical model based...
on an explicit finite difference technique to simulate the heat transfer conditions of a geothermal probe with a U-tube. Authors in [11] carried out a two-dimensional transient model by finite elements to study thermal interference between the U-tubes. Authors in [12] developed an equivalent diameter model for a unique borehole with a U-tube inside. Authors in [13] proposed a three-dimensional implicit finite difference method with a rectangular coordinate system. The similar meshing technique was used in [14]. Authors in [15] developed a three-dimensional unstructured finite volumes model for a unique borehole. The simulation with this model is effective for U-tube geothermal heat exchangers.

In [16], authors proposed an improved finite element model where the well is reduced to a one-dimensional system where the U-shaped loop is replaced by a single pipe of equivalent diameter. Authors in [17] presented an analytical solution to calculate borehole fluid temperatures for time-scales from minutes to decades. Authors in [18] compared different existing approaches for calculating the thermal resistance of the borehole, including the thermal short circuit between the pipes. They also performed a 3D numerical simulation of a drilling well in standard unique U-tube. In [19], authors examined the effects of axial thermal conduction by comparing the results obtained using the finite and infinite linear sources method. Authors in [20] studied the variation of temperature and thermal flux of the borehole wall as a function of time in order to describe the turbulent phenomenon inside the U-tube and to show the temperature distribution in and around the U-tube. Authors in [21] have numerically studied the effect of U-tube diameter, Reynolds number and tube connection configurations on the thermal performance of vertical geothermal heat exchangers. Authors in [22] developed an iterative algorithm to evaluate the thermal performance of GHE by coupling both formulas to calculate the heat transfer rate. The objective of this work is to highlight the effects of flow velocity and materials properties of U-tube, concrete grout and soil on the performance of a geothermal heat exchanger.

II. MATHEMATICAL FORMULATION

The differential equations presented in this paper describe the principle of mass conservation of momentum and energy. In what follows, we will present the formulation describing the phenomenon of forced convection inside the cylindrical pipe and the thermal conduction inside solid media. The discretization of the three-dimensional differential equations of the unsteady flow equation is performed using the finite volume method based on the Fujun algorithm [23]. The differential conservation equations expressed as a function of the different variables of the flow (u, v, w, k, ε, and T) can be written in the following general form [24].

- In vector rotation:
  \[
  \frac{\partial}{\partial t} (\rho \phi) + \text{div} (\rho \cdot U \cdot \phi) = \text{div} (\Gamma_s \cdot \text{grad} \phi) + S_{\phi} \tag{1}
  \]

- In tensor rotation:
  \[
  \frac{\partial}{\partial t} (\rho \phi) + \frac{\partial}{\partial x_j} (\rho \cdot U \cdot \phi) = \frac{\partial}{\partial x_j} \left( \Gamma_s \cdot \frac{\partial \phi}{\partial x_j} \right) + S_{\phi} \tag{2}
  \]

where \( \frac{\partial}{\partial t} (\rho \phi) \) is the foreign exchange rate or accumulation, \( \frac{\partial}{\partial x_j} (\rho \cdot U \cdot \phi) \) the convection flux and \( \frac{\partial}{\partial x_j} \left( \Gamma_s \cdot \frac{\partial \phi}{\partial x_j} \right) \) the diffusion flux. The differential equation describing conservation of momentum for a Newtonian fluid flow is written as:

\[
\rho \left( \frac{\partial U_i}{\partial t} + U_j \frac{\partial U_i}{\partial x_j} \right) = -\frac{\partial P}{\partial x_i} + \mu \left( \frac{\partial^2 U_i}{\partial x_j^2} + \frac{\partial^2 U_i}{\partial x_j \partial x_j} \right) \tag{3}
\]

The equation of motion in the x direction is written in the following form:

\[
\frac{\partial}{\partial t} (\rho \cdot U) + \text{div} (\rho \cdot U \cdot U) = \text{div} \left( \mu \cdot \text{grad} U \right) - \frac{\partial P}{\partial x} + B_x \tag{4}
\]

The differential equation describing the principle of conservation of mass is:

\[
\frac{\partial}{\partial t} (\rho \cdot U) + \frac{\partial}{\partial x_j} (\rho \cdot U_j) = \frac{\partial}{\partial x_j} \rho \epsilon \cdot \text{grad} \psi + \frac{\partial}{\partial x_j} (\rho \cdot U_j) = 0 \tag{5}
\]

Two transport equations in the k-ε model are used, (6) for the kinetic energy of turbulence k obtained from an exact equation and (7) for the rate of kinetic energy dissipation ε obtained by physical resonance.

\[
\frac{\partial}{\partial t} (\rho k) + \frac{\partial}{\partial x_j} \left( \rho \cdot U_j \cdot k \right) = \mu \left( \frac{\partial^2 k}{\partial x_l^2} + \frac{\partial^2 k}{\partial x_j \partial x_j} \right) + G_k + G_v - \rho \epsilon + S_k \tag{6}
\]

\[
\frac{\partial}{\partial t} (\rho \epsilon) + \frac{\partial}{\partial x_j} \left( \rho \cdot U_j \cdot \epsilon \right) = \frac{\partial}{\partial x_j} \left( \mu \frac{\partial \epsilon}{\partial x_j} \right) + \frac{\partial}{\partial x_j} \left( \rho \frac{\partial \epsilon}{\partial x_j} \right) - C_\mu \frac{\epsilon}{k} \left( G_k + C_{\text{st}} G_v \right) - C_\epsilon \rho \frac{\epsilon^2}{K} + S_\epsilon \tag{7}
\]

where \( \sigma_k \) and \( \sigma_\epsilon \) are the Prandtl numbers of \( \kappa \) and \( \epsilon \) with values of 1.0 and 1.2 respectively. \( S_k \) and \( S_\epsilon \) are the terms source, \( C_{\text{st}} \cdot C_{\text{tw}} \) and \( C_{\text{tw}} \) are empirical constants (in this case \( C_{\text{st}} = 1.44, C_{\text{tw}} = 1.92 \)) [25, 27]. The turbulent viscosity is given by:

\[
\mu_t = \rho C_{\mu} \frac{k^2}{\epsilon} \tag{8}
\]

where \( C_{\mu} = 0.09 \).

The energy equation contains a large number of influencing parameters. Taking as simplifying hypothesis chosen in the
elaboration of our numerical model the form of the equation where \( \rho \) and \( \lambda \) (thermal conductivity coefficient) are constant. For the unsteady flow where the viscous dissipation is neglected the equation is written as:

\[
div(\rho \cdot U \cdot h) = div(\lambda \cdot \text{grad} T) + S_h
\]  
(9)

The boundary conditions at the interface are imposed simultaneously in the fluid and solid domains. According to the Fourier law of conductive heat transfer, the term \( \text{div}(\lambda \cdot \text{grad} T) \) represents the influence of heat by conduction in the flow. For ideal gases and for solids and liquids one can write:

\[
C_p \cdot \text{grad} T = \text{grad} h
\]  
(10)

In our case where \( C_p \) is constant, the relationship \( h=f(t) \) is

\[
h = C_p \cdot T
\]  
(11)

III. NUMERICAL PROCEDURE

A. Resolution Method

In general, the method for solving the problem of fluid mechanics or heat transfer follows the procedure illustrated by the flowchart in Figure 2. It can be carried out in three steps:

1. Construction of the geometric model and mesh using the Gambit software.
2. Input of boundary conditions and material properties and resolution of equations using Fluent software.
3. Post-processing of the obtained results.

B. Model of Validation

In order to validate the studied model, we used in a first approach the same model with [28] (see Figure 3). The geometry analyzed is a 5m slice of a geothermal heat exchanger (GHE) inserted into a borehole. It consists of a single U-tube 0.11m in diameter. The model shown in Figure 3 includes three main areas: tube, grout and natural soil. Model construction is done using Gambit software while numerical simulations are performed by Fluent software.

C. Geometric and Thermal Parameters

The parameters determining the geometric and thermal characteristics of the GHE are given in Table I. A time step of 1h has been taken a heat storage time of 700h.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Drilling diameter</td>
<td>0.110</td>
<td>m</td>
</tr>
<tr>
<td>Outside diameter of U pipes</td>
<td>0.032</td>
<td>m</td>
</tr>
<tr>
<td>Distance between pipe centers</td>
<td>0.060</td>
<td>m</td>
</tr>
<tr>
<td>No of pipes in the borehole</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>Conductivity of the soil</td>
<td>3.5</td>
<td>W/mK</td>
</tr>
<tr>
<td>Conductivity of the grout</td>
<td>1.3</td>
<td>W/mK</td>
</tr>
<tr>
<td>Diffusivity of the soil</td>
<td>1.62×10⁻⁶</td>
<td>m²/s</td>
</tr>
<tr>
<td>Diffusivity of the grout</td>
<td>3.33×10⁻⁷</td>
<td>m²/s</td>
</tr>
</tbody>
</table>

D. Physical Parameters

Soil and upper soil surface temperatures as well as the flux density imposed in [28] on the two pipe lugs are entered as calculation input data whose temperature is 10°C and the flux density is 300W/m². The thermo-physical properties (Cp, \( \mu \), k, \( \rho \) et Tin) of the fluid and solids are considered constants. The physical parameters of the materials considered for the validation of our model are presented in Table II.

<table>
<thead>
<tr>
<th>Materials</th>
<th>Thermal conductivity (W/mK)</th>
<th>Density (Kg/m³)</th>
<th>Specific heat capacity (J/Kg°K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Soil</td>
<td>3.5</td>
<td>2360</td>
<td>915</td>
</tr>
<tr>
<td>Grout (concrete)</td>
<td>1.3</td>
<td>2500</td>
<td>1361</td>
</tr>
<tr>
<td>U-tube (HDPE)</td>
<td>0.48</td>
<td>1100</td>
<td>1465</td>
</tr>
</tbody>
</table>
E. Study of Mesh Sensitivity and Validation

In order to study the mesh sensitivity and validate our numerical model, three tests with different meshes were carried out. Figure 4 shows the selected mesh (mesh 3). The results obtained from the evolution of the concrete wall temperature as a function of time were compared with the numerical and analytical results of [28] as shown in Figure 4. Maximum temperatures obtained for each mesh are as follows: mesh 1: 293.72°K, mesh 2: 293.85°K, mesh 3: 294.04°K, while the result obtained in [28] is 294°K. Therefore, we can notice that the closest to [28] result is the one obtained by the mesh 3 and consequently, this one will be used for the numerical simulation of the geothermal vertical U-tube heat exchanger. Figure 5 shows the evolution of the temperature of the concrete wall as a function of time. It can be seen that the curve obtained by the numerical model developed is in good agreement with that obtained analytically and numerically in [28]. In fact, the temperature of the concrete wall increases from 10°C (283°K) to 21°C (294°K) after 700h.

IV. NUMERICAL MODELING OF THE STUDIED GHE

A. Geometrical Configuration

The geometrical configuration of the studied model of GHE is presented in Figure 6. It consists of U-tube with 32mm diameter, 0.06m distance between its two legs, fixed via concrete vertically inside the borehole of 0.11m diameter and depth of 8m. The diameter of the surrounding soil is 6m and the depth is 8m.

B. Physical Parameters and Boundary Conditions

The physical parameters are the same as that used by authors in [28] (see Tables I and II). Noting that in this simulation, the full model is used taking into account the thermal and dynamic effects and consequently other parameters have been added, such as, the fluid mass flow rate (0.3Kg/s) and the temperature of the inlet fluid (300°K). These parameters are taken from [29]. The details of the initial and boundary conditions are:

- The velocity is maximum at the center of the tube in the z direction.
- The upper surface is defined as an adiabatic wall.
- At the outer edge of the domain, a temperature condition has been imposed. The surface is also defined as a solid wall at a constant temperature of 283°K, the groundwater flow was considered negligible.

C. Mesh of the Model

It is important to note that the definition of geometry and the way in which it is realized is the fundamental point of this work, since the vertical geothermal heat exchanger is built from several volumes that can be assembled to form the desired computational domain. The realized volumes are meshed, then recorded under the .dbs extension of Gambit. In this numerical
simulation, a hybrid mesh with tetrahedron, hexahedron and wedge element was used as shown in Figure 7. It should be noted that this type of mesh is considered being more convenient for heat transfer analysis in GHE [20]. The Fluent software [30] was used for modeling, visualization and analysis of fluid flows and heat transfer using the finite volume method. The model resolution is performed in double precision.

Fig. 7.  Numerical mesh used for the studied model illustrating: (a) the various fields of calculation, (b) the upper and (b) lower parts of GHE.

V. RESULTS AND DISCUSSION

A. Effect of U-tube Material

In order to demonstrate the effect of the U-tube material on the evolution of the concrete wall temperature and the heat flow, five different materials were tested. The physical properties of these materials are shown in Table III. The obtained results for temperature and heat flow as a function of time are presented in Figures 8 and 9 respectively. The same variation trends were noticed for the five different materials. From Figure 8, we can see that the temperature increases rapidly at the beginning (until t~25h), afterwards a small change was observed. This is certainly due to the forced convection of the water to the tube, then the temperature increases slowly by conduction between the U-tube and the concrete grout. From Figure 9, it can be seen that the heat flux decreases very rapidly at the beginning, then a slight variation was noted afterwards for the five different types of U-tube material. From the results obtained, it can be noted that the maximum values of the temperature ($T_{\text{max}}=295^\circ K$) and flux ($\Phi_{\text{max}}= 87.54\text{W/m}^2$) are obtained for the steel tube. While for polymers the best results are obtained for HDPE1 with a temperature $T_{\text{max}}=293.97^\circ K$ and a flux $\Phi_{\text{max}}=172.4\text{W/m}^2$. Knowing that the thermal storage depends on the physical properties of the ground but also on its moisture content and water migrations which have a significant impact on the system efficiency, then, to avoid problems of corrosion of the steels because of water particles that come into solution with these materials, it is recommended to use HDPE1 because it is a better heat carrier.

TABLE III. PHYSICAL PROPERTIES OF THE DIFFERENT MATERIALS STUDIED FOR THE U-TUBE.

<table>
<thead>
<tr>
<th>Tube materials</th>
<th>Thermal conductivity (W/m°K)</th>
<th>Density (Kg/m³)</th>
<th>Specific heat capacity (J/Kg°K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HDPE1 [28]</td>
<td>0.48</td>
<td>1100</td>
<td>1465</td>
</tr>
<tr>
<td>HDPE2 [31]</td>
<td>0.35</td>
<td>2300</td>
<td>920</td>
</tr>
<tr>
<td>Stainless steel [31]</td>
<td>13.8</td>
<td>460</td>
<td>7817</td>
</tr>
<tr>
<td>Polyvinyl chloride [31]</td>
<td>0.15</td>
<td>960</td>
<td>1380</td>
</tr>
</tbody>
</table>

Fig. 8. Evolution of the concrete wall temperature of the geothermal heat exchanger as a function of time for five different materials of U-tube.

B. Effect of the Grout Material

To study the effect of the grout material on the evolution of temperature and flux, four different types of concrete were tested. Table IV gives the values of thermal conductivity, density, and thermal capacity of these materials. To make a comparison of the temperature distribution, we have created a flat surface along the y-axis that divides the model of the geothermal heat exchanger in two parts for the four different types of concrete (Figure 10). On the basis of the numerical simulation coupled in fluid-solid 3D we presented the configurations of the distribution of the temperature for the four types of the concrete. Note that the latter is maximum in the middle of the tubes of the exchanger and decreases while moving away from the tube to the ground. By comparing the temperature distributions for the four types of concrete, it can
be concluded that best results are obtained with concrete 2, while the worst ones are obtained with concrete 3.

**TABLE IV. PHYSICAL PROPERTIES OF THE DIFFERENT MATERIALS STUDIED FOR GROUTING CONCRETE.**

<table>
<thead>
<tr>
<th>Grout materials</th>
<th>Thermal conductivity (W/m°K)</th>
<th>Density (Kg/m³)</th>
<th>Specific heat capacity (J/Kg°K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concrete 1</td>
<td>1.3</td>
<td>2500</td>
<td>1561</td>
</tr>
<tr>
<td>Concrete 2</td>
<td>1.4</td>
<td>2210</td>
<td>750</td>
</tr>
<tr>
<td>Concrete 3</td>
<td>0.6</td>
<td>1420</td>
<td>1197</td>
</tr>
<tr>
<td>(Silica sand)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Concrete 4</td>
<td>1</td>
<td>1500</td>
<td>1600</td>
</tr>
<tr>
<td>(Sand bentonite)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Fig. 10. Temperature distribution for the four types of concrete.

Figures 11 and 12 respectively show the evolutions of the temperature and heat flow of the concrete wall as a function of time during 700 hours of operation for four types of concrete using a U-tube in HDPE1. It should be noted that the main objective in this section is to determine the appropriate concrete with the material chosen for the pipe in HDPE1. By comparing the results obtained for the four types of concrete, it can be noted that the best thermal performance is obtained by concrete 2. Indeed, the maximum values of the temperature and the flux for this type of concrete are respectively 294.2°K and 175.4W/m². In addition, it can be noted that the results closest to those of concrete 2 are those of concrete 1 where the temperature is 94°K with a flux of 172.4W/m². Concrete 3 performs poorly.

**C. Effect of the Soil Properties**

In this section we will focus on the choice of soil that allows us to obtain the best thermal performance from an energy storage point of view. To do this, six different types of soil will be tested. The thermal properties of these soils are presented in Table V. The temperature distributions in the U-tube geothermal heat exchanger at the medial surfaces for each soil type are shown in Figure 13. It can be seen that there is a slight difference between the isovalue contours of the temperatures obtained for the six soil types. Best results are obtained by silty clayey sand (Figure 13(f)). The evolution of the borehole wall temperature as a function of time is illustrated in Figure 14. All simulations were made with the optimal parameters obtained previously for the materials of U-tube and concrete. It can be seen that the heat transfer is highly significant in the case of clay sand where the maximum temperature is 297.47°K after 700h. A slight difference compared to the sand was noted where the maximum temperature of the latter is 297.39°K, which means that both soil types have better heat preservation. On the other hand, the type of soil that produces a poor heat conservator is shale where the maximum temperature does not exceed 294.76°K.

**TABLE V. PHYSICAL PROPERTIES OF THE STUDIED SOIL TYPES**

<table>
<thead>
<tr>
<th>Soil materials</th>
<th>Thermal conductivity (W/m°K)</th>
<th>Density (Kg/m³)</th>
<th>Specific heat capacity (J/Kg°K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Clay [31]</td>
<td>1.2</td>
<td>1700</td>
<td>1800</td>
</tr>
<tr>
<td>Sandy Clay [31]</td>
<td>2.1</td>
<td>1960</td>
<td>1200</td>
</tr>
<tr>
<td>Sand [31]</td>
<td>1.1</td>
<td>1510</td>
<td>1100</td>
</tr>
<tr>
<td>Silty clayey sand [34]</td>
<td>1</td>
<td>1900</td>
<td>1500</td>
</tr>
<tr>
<td>Shale [34]</td>
<td>2.9</td>
<td>2400</td>
<td>1200</td>
</tr>
<tr>
<td>Sandy silt [35]</td>
<td>1.3</td>
<td>1847</td>
<td>1200</td>
</tr>
</tbody>
</table>

**D. Effect of Flow Velocity**

To study the influence of the fluid (water) velocity on the thermal storage in the soil, five different velocities \(U=\{0.173, 0.273, 0.373, 0.473 \text{ and } 0.573 \text{ m/s}\}\) were tested using the previously selected materials for three components of the geothermal heat exchanger. The choice of these velocity values was based on [28], in which the velocity used was 0.373m/s. A change of ±0.1m/s has been added to this value. The results obtained for the evolution of the temperature of the concrete wall as a function of time for different water flow speeds are...
illustrated in Figure 15. It may be noted that as the flow velocity increases, the temperature rises, but this increase is not significant. Indeed, for a speed of 0.137 m/s (minimum speed studied) the maximum temperature is 297.36°K, while for a speed of 0.537 m/s (maximum speed studied) the maximum temperature is 297.5°K, meaning that a difference of 0.05% was found.

Fig. 13. Contour plots of the temperature distribution for the six soil types.

Figure 14 shows the velocity vectors stained by the amplitude of the velocity. Increasing of the fluid velocity increases the intensity of the turbulence which causes the increase in forced convection heat transfer between the water and the U-tube wall. The heat that is released is transferred by conduction to the concrete wall which makes the temperature of the latter higher. It can be seen in Figure 13 that the velocity is maximum at the upper part at the beginning of the U-tube bend. The water is accelerated down until it reaches the elbow and then it slows down until it reaches its initial velocity of entry at the outlet of the U-tube. It should be noted that the magnitude of the velocity at the inlet and outlet of the tube is 0.373 m/s. The magnitude of the velocity at the entrance of the elbow reached 0.573 m/s.

Fig. 14. Evolution of the temperature in the radial GHE direction.

E. GHE Temperature Distribution in the Depth Direction

After the optimization of the material properties, in this section, we focus to highlight the temperature distribution along the depth of the GHE. Figures 17 and 18 show the evolution of the temperature field inside the borehole along the radial direction of the GHE at different depths (z=0, 2.5, 4.5 and 5.0 m) for heat storage time of 700 h. It can be seen that with increasing depth, the temperature in the radial direction gradually rises. Furthermore, a slight difference has been found between the temperature distribution for 2.5 m and 4.5 m or 5 m. In addition, a symmetric distribution is noticed between the inlet branch part (to the left) and the outlet branch part (to the right) of the U-tube. This is because these illustrations were taken after the equilibrium state and the stability of the temperature distribution in the GHE (700 h).

Fig. 15. Evolution of the borehole wall temperature for different water velocities.

Fig. 16. Continuity and direction of the fluid flow.

Fig. 17. Evolution of the temperature in the radial GHE direction.
VI. CONCLUSION

This study was dedicated to the optimization of solar energy storage systems based on a thermodynamic simulation of a U-tube vertical geothermal heat exchanger buried in concrete grout and soil. The 3D numerical simulation was based on forced convection and conduction in an unsteady flow. From the results presented in this numerical investigation, we can draw the following conclusions: (a) An acceptable agreement was found between the developed model validation results and those of the literature. (b) A slight influence of fluid flow velocity on energy conservation performance has been found. (c) To obtain the best performance for the developed geothermal heat exchanger model, it is recommended to use (i) a U-tube made of HDPE1 (thermal conductivity 0.48W/m·K, density 1100Kg/m³ and a mass thermal capacity of 14655J/Kg°C), (ii) type 2 concrete (with high thermal conductivity and low specific heat capacity) for grout, (iii) clay sand as burial soil. The higher the soil thermal conductivity, the lower the temperature damping.

TABLE VI. NOMENCLATURE

<table>
<thead>
<tr>
<th>$C_{x}$, $C_{y}$, $C_{z}$, $b_{i}$</th>
<th>Constants used in the standard $k$-model</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{p}$</td>
<td>Specific heat (J/kgK)</td>
</tr>
<tr>
<td>$G$</td>
<td>The turbulent flow production term</td>
</tr>
<tr>
<td>$h$</td>
<td>Enthalpy (J/kg)</td>
</tr>
<tr>
<td>$K$</td>
<td>Thermal conductivity (W/mK)</td>
</tr>
<tr>
<td>$S_{x}$, $S_{y}$, $S_{z}$</td>
<td>Sources terms</td>
</tr>
<tr>
<td>$T$</td>
<td>Temperature (°K)</td>
</tr>
<tr>
<td>$P$</td>
<td>Static pressure</td>
</tr>
<tr>
<td>$U$</td>
<td>Fluid velocity in the x-direction (m/s)</td>
</tr>
<tr>
<td>$V$</td>
<td>Fluid velocity in the y-direction (m/s)</td>
</tr>
<tr>
<td>$W$</td>
<td>Fluid velocity in the z-direction (m/s)</td>
</tr>
<tr>
<td>$x$, $y$, $z$</td>
<td>Cartesian coordinates (m)</td>
</tr>
<tr>
<td>$\varepsilon$</td>
<td>Dissipation rate of turbulence energy (m²/s)</td>
</tr>
<tr>
<td>$\varphi$</td>
<td>General dependent variable</td>
</tr>
<tr>
<td>$\Gamma$</td>
<td>Diffusion coefficient</td>
</tr>
<tr>
<td>$k$</td>
<td>Turbulent kinetic energy (m²/s)</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>Coefficient of thermal conductivity</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Dynamic viscosity (Pa·s)</td>
</tr>
<tr>
<td>$\mu_{t}$</td>
<td>Turbulent viscosity (Pa·s)</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Density (kg/m³)</td>
</tr>
<tr>
<td>$\sigma_{x}$</td>
<td>Prandtl number of $\varepsilon$</td>
</tr>
<tr>
<td>$\sigma_{z}$</td>
<td>Prandtl number of $K$</td>
</tr>
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</table>

REFERENCES


